## vDSP Matrix Operations Reference

Performance > Carbon

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# vDSP Matrix Operations Reference 

| Framework: | Accelerate/vecLib |
| :--- | :--- |
| Declared in | vDSP.h |

## Overview

This document describes the C API for the matrix arithmetic operations available in vDSP. It provides functionality for multiplying and transposing real or complex matrices.

## Functions by Task

## Multiplying Real Matrices

## vDSP_mmul (page 8)

Performs an out-of-place multiplication of M-by-P matrix $A$ by a P-by-N matrix $B$ and stores the results in an M-by-N matrix $C$; single precision.
vDSP_mmulD (page 9)
Performs an out-of-place multiplication of M-by-P matrix $A$ by a P-by-N matrix $B$ and stores the results in an $M$-by- $N$ matrix C; double precision.

## Transposing a Matrix

vDSP_mtrans (page 9)
Creates a transposed matrix C from a source matrix A; single precision.
vDSP_mtransD (page 10)
Creates a transposed matrix C from a source matrix A; double precision.

## Copying a Submatrix

```
vDSP_mmov (page 6)
    The contents of a submatrix are copied to another submatrix.
vDSP_mmovD (page 7)
The contents of a submatrix are copied to another submatrix.
```


## Multiplying Complex Matrices

vDSP_zmma (page 10)
Performs an out-of-place complex multiplication of an M-by-P matrix A by a P-by-N matrix B, adds the product to $M$-by- $N$ matrix $C$, and stores the result in $M$-by- $N$ matrix $D$; single precision.
vDSP_zmmaD (page 11)
Performs an out-of-place complex multiplication of an M-by-P matrix A by a P-by-N matrix B, adds the product to $M$-by-N matrix $C$, and stores the result in $M-b y-N$ matrix $D$; double precision.
vDSP_zmms (page 12)
Performs an out-of-place complex multiplication of an M-by-P matrix A by a P-by-N matrix B , subtracts $M$-by-N matrix $C$ from the product, and stores the result in $M-b y-N$ matrix $D$; single precision.
vDSP_zmmsD (page 13)
Performs an out-of-place complex multiplication of an M-by-P matrix A by a P-by-N matrix B , subtracts M-by-N matrix C from the product, and stores the result in M-by-N matrix D; double precision.
vDSP_zmmul (page 14)
Performs an out-of-place complex multiplication of an M-by-P matrix A by a P-by-N matrix B and stores the results in an $M-b y-N$ matrix $C$; single precision.
vDSP_zmmulD (page 14)
Performs an out-of-place complex multiplication of an M-by-P matrix A by a P-by-N matrix B and stores the results in an M-by-N matrix C; double precision.
vDSP_zmsm (page 15)
Performs an out-of-place complex multiplication of an M-by-P matrix A by a P-by-N matrix B, subtracts the product from M-by-P matrix $C$, and stores the result in $M$-by- $P$ matrix $D$; single precision.
vDSP_zmsmD (page 16)
Performs an out-of-place complex multiplication of an $M-b y-P$ matrix $A$ by a $P-b y-N$ matrix $B$, subtracts the product from M-by-P matrix $C$, and stores the result in $M$-by- $P$ matrix $D$; double precision.

## Functions

## vDSP_mmov

The contents of a submatrix are copied to another submatrix.

```
void
vDSP_mmov (float * A,
float * C,
vDSP_Length NC,
vDSP_Length NR,
vDSP_Length TCA,
vDSP_Length TCC);
```


## Parameters

A
Single-precision real input submatrix
C
Single-precision real output submatrix

NC
Number of columns in $A$ and $C$
NR
Number of rows in $A$ and $C$
TCA
Number of columns in the matrix of which A is a submatrix
TCC
Number of columns in the matrix of which $C$ is a submatrix

## Discussion

The matrices are assumed to be stored in row-major order. Thus elements $A[i][j]$ and $A[i][j+1]$ are adjacent. Elements $A[i][j]$ and $A[i+1][j]$ are TCA elements apart.

This function may be used to move a subarray beginning at any point in a larger embedding array by passing for A the address of the first element of the subarray. For example, to move a subarray starting at A[3][4], pass \& $A[3][4]$. Similarly, the address of the first destination element is passed for $C$

NC may equal TCA, and it may equal TCC. To copy all of an array to all of another array, pass the number of rows in NR and the number of columns in NC, TCA, and TCC.

## Availability

Available in Mac OS X v10.4 and later.

## Declared In

vDSP.h

## vDSP_mmovD

The contents of a submatrix are copied to another submatrix.

```
void vDSP_mmovD (double * A,
double * C,
vDSP_Length NC,
vDSP_Length NR,
vDSP_Length TCA,
vDSP_Length TCC);
```


## Parameters

A
Double-precision real input submatrix
C
Double-precision real output submatrix
NC
Number of columns in A and C
NR
Number of rows in $A$ and $C$

Number of columns in the matrix of which A is a submatrix

Number of columns in the matrix of which $C$ is a submatrix

## Discussion

The matrices are assumed to be stored in row-major order. Thus elements $A[i][j]$ and $A[i][j+1]$ are adjacent. Elements A[i][j] and A[i+1][j] are TCA elements apart.

This function may be used to move a subarray beginning at any point in a larger embedding array by passing for A the address of the first element of the subarray. For example, to move a subarray starting at A[3][4], pass \& A[3][4]. Similarly, the address of the first destination element is passed for $C$

NC may equal TCA, and it may equal TCC. To copy all of an array to all of another array, pass the number of rows in NR and the number of columns in NC, TCA, and TCC.

## Availability

Available in Mac OS X v10.4 and later.

## Declared In

vDSP.h

## vDSP_mmul

Performs an out-of-place multiplication of M-by-P matrix $A$ by a $P$-by- $N$ matrix $B$ and stores the results in an M-by-N matrix C; single precision.

```
void vDSP_mmul (float * A,
vDSP_Stride I,
float * B,
vDSP_Stride J,
float * C,
vDSP_Stride K,
vDSP_Length M,
vDSP_Length N,
vDSP_Length P);
```


## Discussion

This performs the operation
$C_{(m N+n) K}=\sum_{p=0}^{P-1} A_{(m P+p) I} \cdot B_{(p N+n) J} \quad \mathrm{n}=\{0, \mathrm{~N}-1\}$ and $\mathrm{m}=\{0, \mathrm{M}-1\}$

Parameters $A$ and $B$ are the matrixes to be multiplied. I is an address stride through $A . J$ is an address stride through B.

Parameter $C$ is the result matrix. $K$ is an address stride through $C$.
Parameter $M$ is the row count for both $A$ and $C$. Parameter $N$ is the column count for both $B$ and $C$. Parameter $P$ is the column count for $A$ and the row count for $B$.

## Availability

Available in Mac OS X v10.4 and later.

## Declared In

vDSP.h

## vDSP_mmulD

Performs an out-of-place multiplication of M-by-P matrix $A$ by a $P-b y-N$ matrix $B$ and stores the results in an M-by-N matrix C; double precision.

```
void vDSP_mmulD (double * A,
vDSP_Stride I,
double * B,
vDSP_Stride J,
double * C,
vDSP_Stride K,
vDSP_Length M,
vDSP_Length N,
vDSP_Length P);
```


## Discussion

This performs the operation
$C_{(m N+n) K}=\sum_{p=0}^{P-1} A_{(m P+p) I} \cdot B_{(p N+n) J} \quad \mathrm{n}=\{0, \mathrm{~N}-1\}$ and $\mathrm{m}=\{0, \mathrm{M}-1\}$

Parameters $A$ and $B$ are the matrixes to be multiplied. $I$ is an address stride through $A . J$ is an address stride through B.

Parameter $C$ is the result matrix. $K$ is an address stride through $C$.
Parameter $M$ is the row count for both $A$ and $C$. Parameter $N$ is the column count for both $B$ and $C$. Parameter $P$ is the column count for $A$ and the row count for $B$.

## Availability

Available in Mac OS X v10.4 and later.

## Declared In

vDSP.h

## vDSP_mtrans

Creates a transposed matrix $C$ from a source matrix A; single precision.

```
void vDSP_mtrans (float * A,
vDSP_Stride I,
float * C,
vDSP_Stride K,
vDSP_Length M,
vDSP_Length N);
```


## Discussion

This performs the operation
$C_{(m N+n) K}=A_{(n M+m) I} \quad \mathrm{n}=\{0, \mathrm{~N}-1\}$ and $\mathrm{m}=\{0, \mathrm{M}-1\}$

Parameter $A$ is the source matrix. I is an address stride through the source matrix.

Parameter $C$ is the resulting transposed matrix. $K$ is an address stride through the result matrix.
Parameter $M$ is the number of rows in $C$ (and the number of columns in $A$ ).

## Availability

Available in Mac OS X v10.4 and later.

## Declared In

vDSP.h

## vDSP_mtransD

Creates a transposed matrix C from a source matrix A; double precision.

```
void vDSP_mtransD (double * A,
vDSP_Stride I,
doub7e * C,
vDSP_Stride K,
vDSP_Length M,
vDSP_Length N);
```


## Discussion

This performs the operation
$C_{(m N+n) K}=A_{(n M+m) I} \quad \mathrm{n}=\{0, \mathrm{~N}-1\}$ and $\mathrm{m}=\{0, \mathrm{M}-1\}$

Parameter A is the source matrix. I is an address stride through the source matrix.
Parameter $C$ is the resulting transposed matrix. $K$ is an address stride through the result matrix.
Parameter $M$ is the number of rows in $C$ (and the number of columns in $A$ ).

## Availability

Available in Mac OS X v10.4 and later.

## Declared In

vDSP.h

## vDSP_zmma

Performs an out-of-place complex multiplication of an M-by-P matrix A by a P-by-N matrix $B$, adds the product to M-by-N matrix C, and stores the result in M-by-N matrix $D$; single precision.

```
void vDSP_zmma (DSPSplitComplex * A,
vDSP_Stride I,
DSPSplitComplex * B,
vDSP_Stride J,
DSPSplitComplex * C,
vDSP_Stride K,
DSPSplitComplex * D,
vDSP_Stride L,
vDSP_Length M,
vDSP_Length N,
vDSP_Length P);
```


## Discussion

This performs the operation

$$
\begin{aligned}
D_{(r N+q) L}=C_{(r N+q) K} & +\sum_{p=0}^{P-1} A_{(r P+p) I} B_{(p N+q) J} \\
& 0 \leq r<M, \quad 0 \leq q<N
\end{aligned}
$$

Parameters $A$ and $C$ are the matrixes to be multiplied, and $C$ the matrix to be added. I is an address stride through $A . J$ is an address stride through B. $K$ is an address stride through $C . L$ is an address stride through D.

Parameter $D$ is the result matrix.
Parameter $M$ is the row count for $A, C$ and $D$. Parameter $N$ is the column count of $B, C$, and $D$. Parameter $P$ is the column count of $A$ and the row count of $B$.

## Availability

Available in Mac OS X v10.4 and later.

## Declared In

vDSP.h

## vDSP_zmmaD

Performs an out-of-place complex multiplication of an $M$-by-P matrix $A$ by a $P$-by- $N$ matrix $B$, adds the product to $M$-by- $N$ matrix $C$, and stores the result in $M-b y-N$ matrix $D$; double precision.

```
void vDSP_zmmaD (DSPDoubleSplitComplex * A,
vDSP_Stride I,
DSPDoubleSplitComplex * B,
vDSP_Stride J,
DSPDoubleSplitComplex * C,
vDSP_Stride K,
DSPDoubleSplitComplex * D,
vDSP_Stride L,
vDSP_Length M,
vDSP_Length N,
vDSP_Length P);
```


## Discussion

This performs the operation

$$
\begin{aligned}
D_{(r N+q) L}=C_{(r N+q) K} & +\sum_{p=0}^{P-1} A_{(r P+p) I} B_{(p N+q) J} \\
& 0 \leq r<M, \quad 0 \leq q<N
\end{aligned}
$$

Parameters $A$ and $C$ are the matrixes to be multiplied, and $C$ the matrix to be added. I is an address stride through A. $J$ is an address stride through B. $K$ is an address stride through $C . L$ is an address stride through D.

Parameter $D$ is the result matrix.

Parameter $M$ is the row count for $A, C$ and $D$. Parameter $N$ is the column count of $B, C$, and $D$. Parameter $P$ is the column count of $A$ and the row count of $B$.

## Availability

Available in Mac OS X v10.4 and later.

## Declared In

vDSP.h

## vDSP_zmms

Performs an out-of-place complex multiplication of an M-by-P matrix A by a P-by-N matrix B , subtracts M-by-N matrix $C$ from the product, and stores the result in $M-b y-N$ matrix $D$; single precision.

```
void vDSP_zmms (DSPSplitComplex * A,
vDSP_Stride I,
DSPSplitComplex * B,
vDSP_Stride J,
DSPSplitComplex * C,
vDSP_Stride K,
DSPSplitComplex * D,
vDSP_Stride L,
vDSP_Length M,
vDSP_Length N,
vDSP_Length P);
```


## Discussion

This performs the operation

$$
\begin{aligned}
D_{(r N+q) L}= & \sum_{p=0}^{P-1} A_{(r P+p) I} B_{(p N+q) J}-C_{(r N+q) K} \\
& 0 \leq r<M, \quad 0 \leq q<N
\end{aligned}
$$

Parameters $A$ and $B$ are the matrixes to be multiplied, and $C$ the matrix to be subtracted. $I$ is an address stride through $A . J$ is an address stride through $B . K$ is an address stride through $C . L$ is an address stride through D.

Parameter $D$ is the result matrix.

Parameter $M$ is the row count for $A, C$ and $D$. Parameter $N$ is the column count of $B, C$, and $D$. Parameter $P$ is the column count of $A$ and the row count of $B$.

## Availability

Available in Mac OS X v10.4 and later.

## Declared In

vDSP.h

## vDSP_zmmsD

Performs an out-of-place complex multiplication of an M-by-P matrix A by a P-by-N matrix B , subtracts M-by-N matrix $C$ from the product, and stores the result in $M$-by-N matrix $D$; double precision.

```
void vDSP_zmmsD (DSPDoubleSplitComplex * A,
vDSP_Stride I,
DSPDoubleSplitComplex * B,
vDSP_Stride J,
DSPDoubleSplitComplex * C,
vDSP_Stride K,
DSPDoubleSplitComplex * D,
vDSP_Stride L,
vDSP_Length M,
vDSP_Length N,
vDSP_Length P);
```


## Discussion

This performs the operation
$D_{(r N+q) L}=\sum_{p=0}^{P-1} A_{(r P+p) I} B_{(p N+q) J}-C_{(r N+q) K}$
$0 \leq r<M, \quad 0 \leq q<N$

Parameters $A$ and $B$ are the matrixes to be multiplied, and $C$ the matrix to be subtracted. $I$ is an address stride through $A . J$ is an address stride through $B . K$ is an address stride through $C . L$ is an address stride through D.

Parameter $D$ is the result matrix.
Parameter $M$ is the row count for $A, C$ and $D$. Parameter $N$ is the column count of $B, C$, and $D$. Parameter $P$ is the column count of $A$ and the row count of $B$.

## Availability

Available in Mac OS X v10.4 and later.

## Declared In

vDSP.h

## vDSP_zmmul

Performs an out-of-place complex multiplication of an M-by-P matrix A by a P-by-N matrix B and stores the results in an M-by-N matrix C; single precision.

```
void vDSP_zmmul (DSPSplitComplex * A,
vDSP_Stride I,
DSPSplitComplex * B,
vDSP_Stride J,
DSPSplitComplex * C,
vDSP_Stride K,
vDSP_Length M,
vDSP_Length N,
vDSP_Length P);
```


## Discussion

This performs the operation
$C_{(m N+n) K}=\sum_{p=0}^{P-1} A_{(m P+p) I} \cdot B_{(p N+n) J} \quad \mathrm{n}=\{0, \mathrm{~N}-1\}$ and $\mathrm{m}=\{0, \mathrm{M}-1\}$

Parameters $A$ and $B$ are the matrixes to be multiplied. I is an address stride through $A$. $J$ is an address stride through B.

Parameter $C$ is the result matrix. $K$ is an address stride through $C$.
Parameter $M$ is the row count for both $A$ and $C$. Parameter $N$ is the column count for both B and C. Parameter $P$ is the column count for $A$ and the row count for $B$.

## Availability

Available in Mac OS X v10.4 and later.

## Declared In

vDSP.h

## vDSP_zmmulD

Performs an out-of-place complex multiplication of an M-by-P matrix A by a P-by-N matrix B and stores the results in an M-by-N matrix C; double precision.

```
void vDSP_zmmulD (DSPDoubleSplitComplex * A,
vDSP_Stride I,
DSPDoubleSplitComplex * B,
vDSP_Stride J,
DSPDoubleSplitComplex * C,
vDSP_Stride K,
vDSP_Length M,
vDSP_Length N,
vDSP_Length P);
```


## Discussion

This performs the operation
$C_{(m N+n) K}=\sum_{p=0}^{P-1} A_{(m P+p) I} \cdot B_{(p N+n) J} \quad \mathrm{n}=\{0, \mathrm{~N}-1\}$ and $\mathrm{m}=\{0, \mathrm{M}-1\}$

Parameters $A$ and $B$ are the matrixes to be multiplied. I is an address stride through $A . J$ is an address stride through B.

Parameter $C$ is the result matrix. $K$ is an address stride through $C$.
Parameter $M$ is the row count for both $A$ and $C$. Parameter $N$ is the column count for both $B$ and $C$. Parameter $P$ is the column count for $A$ and the row count for $B$.

## Availability

Available in Mac OS X v10.4 and later.

## Declared In

vDSP.h

## vDSP_zmsm

Performs an out-of-place complex multiplication of an M-by-P matrix A by a P-by-N matrix B, subtracts the product from $M$-by- $P$ matrix $C$, and stores the result in $M$-by- $P$ matrix $D$; single precision.

```
void vDSP_zmsm (DSPSplitComplex * A,
vDSP_Stride I,
DSPSplitComplex * B,
vDSP_Stride J,
DSPSplitComplex * C,
vDSP_Stride K,
DSPSplitComplex * D,
vDSP_Stride L,
vDSP_Length M,
vDSP_Length N,
vDSP_Length P);
```


## Discussion

This performs the operation
$D_{(r N+q) L}=C_{(r N+q) K}-\sum_{p=0}^{P-1} A_{(r P+p) I} B_{(p N+q) J}$

Parameters $A$ and $B$ are the matrixes to be multiplied, and $C$ is the matrix from which the product is to be subtracted. aStride is an address stride through A.bStride is an address stride through B. cStride is an address stride through C. dStride is an address stride through D.

Parameter $D$ is the result matrix.
Parameter $M$ is the row count for $A, C$ and $D$. Parameter $N$ is the column count of $B, C$, and $D$. Parameter $P$ is the column count of $A$ and the row count of $B$.

## Availability

Available in Mac OS X v10.4 and later.

## Declared In

vDSP.h

## vDSP_zmsmD

Performs an out-of-place complex multiplication of an M-by-P matrix A by a P-by-N matrix B, subtracts the product from M-by-P matrix $C$, and stores the result in $M$-by- $P$ matrix $D$; double precision.

```
void vDSP_zmsmD (DSPDoubleSplitComplex * A,
vDSP_Stride I,
DSPDoubleSplitComplex * B,
vDSP_Stride J,
DSPDoubleSplitComplex * C,
vDSP_Stride K,
DSPDoubleSplitComplex * D,
vDSP_Stride L,
vDSP_Length M,
vDSP_Length N,
vDSP_Length P);
```


## Discussion

This performs the operation
$D_{(r N+q) L}=C_{(r N+q) K}-\sum_{p=0}^{P-1} A_{(r P+p) I} B_{(p N+q) J}$

Parameters $A$ and $B$ are the matrixes to be multiplied, and parameter $C$ is the matrix from which the product is to be subtracted. aStride is an address stride through A. bStride is an address stride through B. cStride is an address stride through C. dStride is an address stride through D.

Parameter $D$ is the result matrix.

Parameter $M$ is the row count for $A, C$ and $D$. Parameter $N$ is the column count of $B, C$, and $D$. Parameter $P$ is the column count of $A$ and the row count of $B$.

## Availability

Available in Mac OS X v10.4 and later.

Declared In
vDSP.h

## Document Revision History

This table describes the changes to vDSP Matrix Operations Reference.

| Date | Notes |
| :--- | :--- |
| 2009-01-06 | Includes vDSP_mmov and vDSP_mmovD. |
| 2007-06-15 | New document that describes the C API for the vDSP functionality for matrix <br> operations. |

Document Revision History

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